# UNIVERSITY OF MADRAS

# B.Sc. DEGREE COURSE IN MATHEMATICS SYLLABUS WITH EFFECT FROM 2020-2021

BMA-CSC15

# CORE-XV: COMPLEX ANALYSIS

(Common to B.Sc. Maths with Computer Applications)

Inst.Hrs: 6

Credits: 4

YEAR: III
SEMESTER: VI

# **Learning outcomes:**

Students will acquire knowledge about the basic ideas of analysis of Complex Functions in solving Complex Variables.

#### UNIT I

Analytic Functions: Functions of a Complex Variable – Limit- Theorems on Limits – Continuous functions- Differentiability – Cauchy – Riemann equations – Analytic functions-Harmonic functions – Conformal mapping.

Chapter  $1 - \sec 2.1$  to 2.9.

## **UNIT II**

Bilinear Transformations:Elementary transformations – Bilinear transformations – Cross ratio-Fixed Points of Bilinear Transformations – Mapping by Elementary Functions – The Mapping  $w=z^2,\,z^n,\,n$  is a positive integer,  $w=e^z,\,\sin z,\,\cos z$ .

Chapter  $3 - \sec 3.1$  to 3.4, Chapter  $5 - \sec 5.1$  to 5.5

#### UNIT III

Complex Integration – definite integral – Cauchy's Theorem – Cauchy's integral formula – Higher derivatives. Chapter 6 – sec 6.1 to 6.4

# **UNIT IV**

Series expansions – Taylor's series – Laurent's Series – Zeroes of analytic functions-Singularities. Chapter 7-7.1 to 7.4

#### **UNIT V**

Residues — Cauchy's Residue Theorem — Evaluation of definite integrals. Chapter 8-8.1 to 8.3.

#### Content and treatment as in

"Complex Analysis" byDr.S.Arumugam,Thangapandi Isaac, Dr.A.Somasundaram, SciTech publications(India) Pvt Ltd,2002.

#### **Reference:**

- 1. Complex variables and Applications (Sixth Edition) by James Ward Brown and RuelV.Churchill, Mc.Grawhill Inc.
- 2. Complex Analysis by P.Duraipandian, Kayalak Pachaiyappa, S. Chand & Co Pvt. Ltd.
- 3. Complex Analysis ,T.K.Manickavachagom Pillay, S.Viswanathan Publishers Pvt. Ltd.

## e-Resources:

- 1. http://ebooks.lpude.in.complexanalysis.
- 2. <a href="https://nptel.ac.in">https://nptel.ac.in</a>.